

Principles of Communications

ECS 332

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6. Sampling and Reconstruction



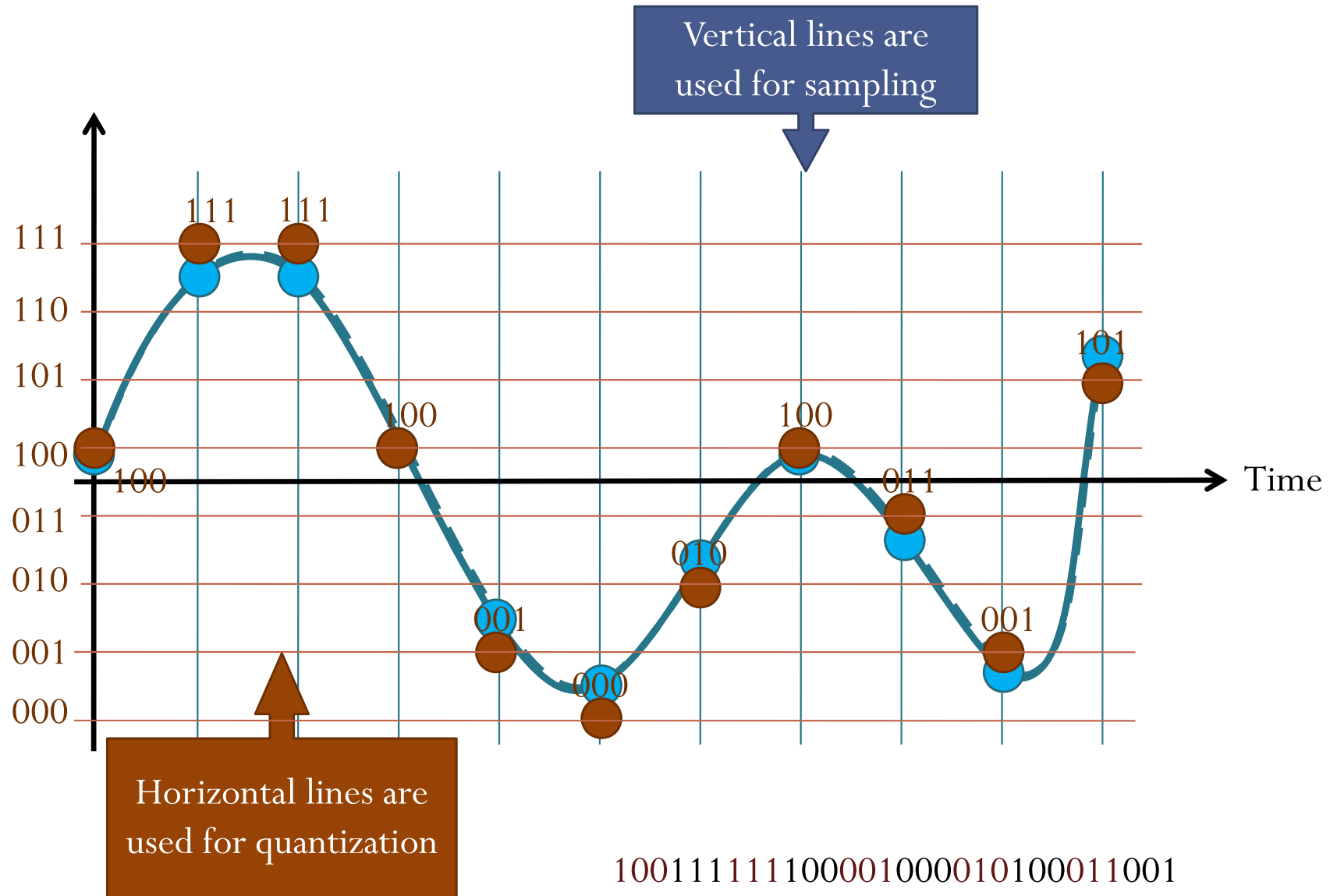
Office Hours:

BKD, 6th floor of Sirindhralai building

Wednesday 14:00-15:30

Friday 14:00-15:30

Digitization (analog to digital)



Principles of Communications

ECS 332

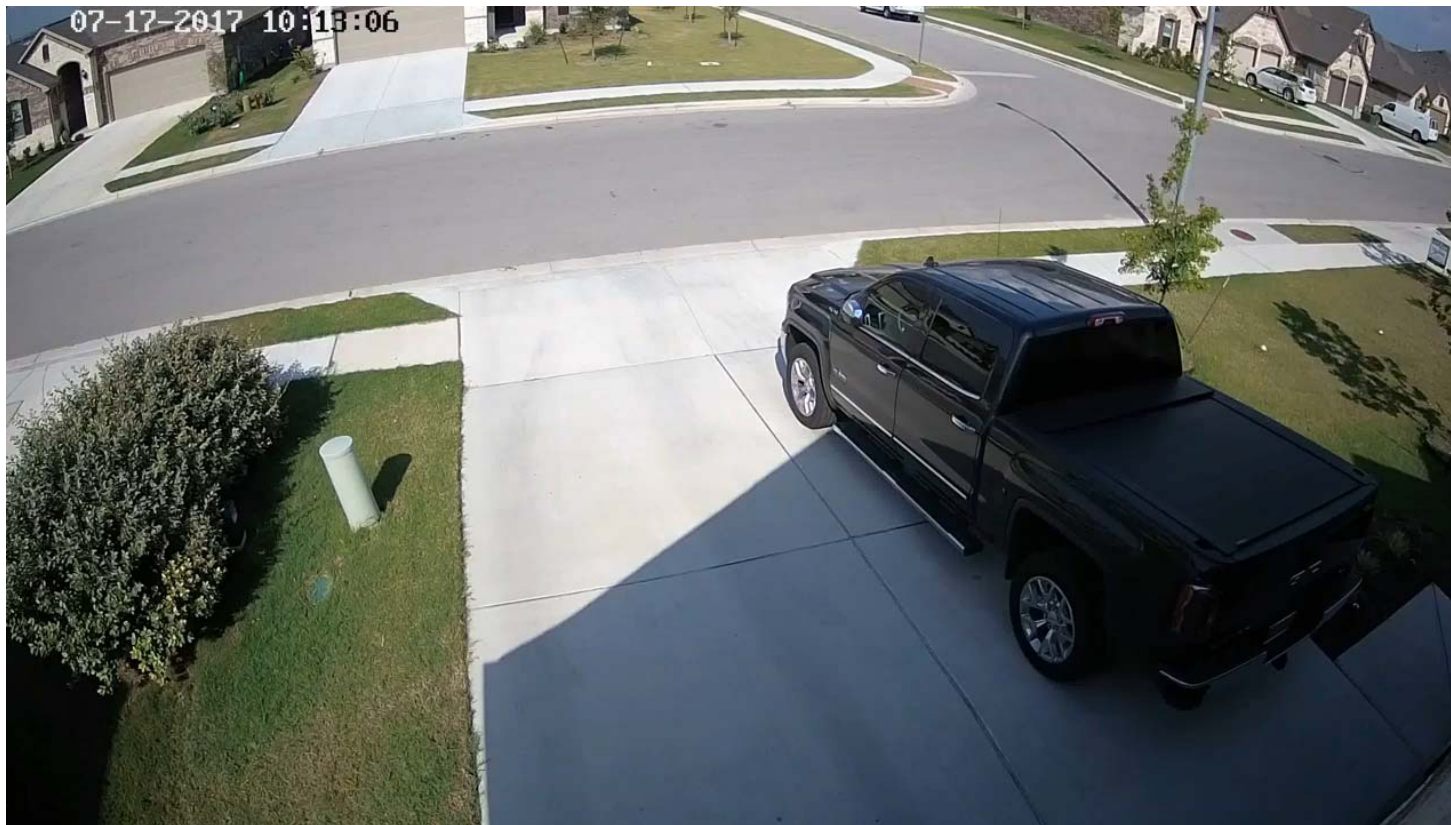
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6.1 Sampling

A bird's mind-boggling stunt?

- Viewed over 250k times in just 24 hours after a YouTuber uploaded it to the internet.



[http://www.boredpanda.com/camera-frame-rate-synced-bird-wings/?utm_source=CB11&utm_medium=link&utm_campaign=SAW]

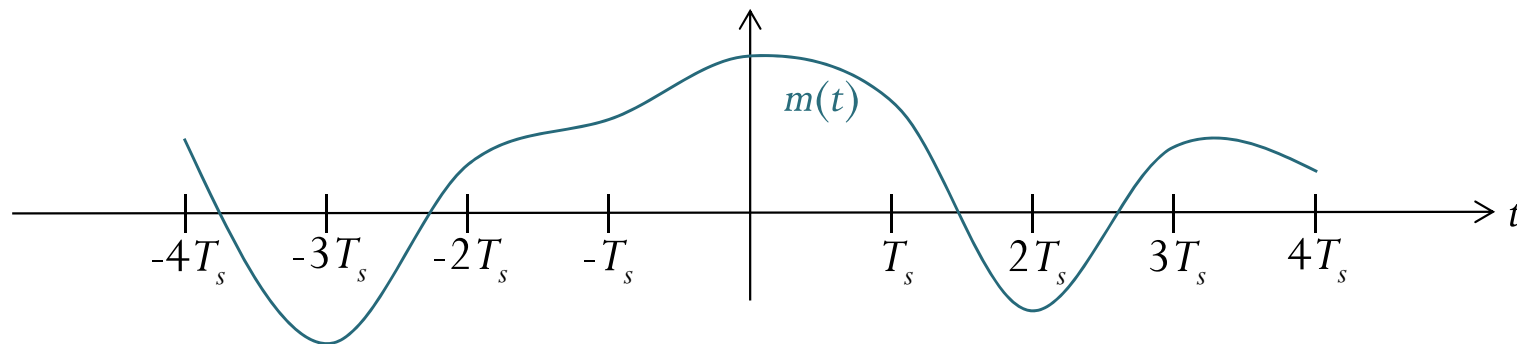


A magically hovering helicopter?



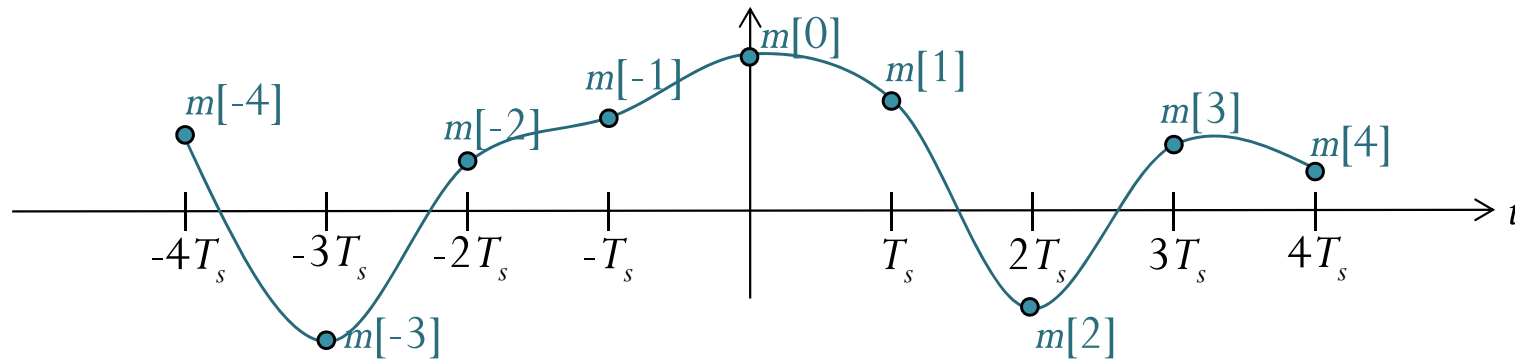
Sampling

- Start with a continuous-time (analog) signal.



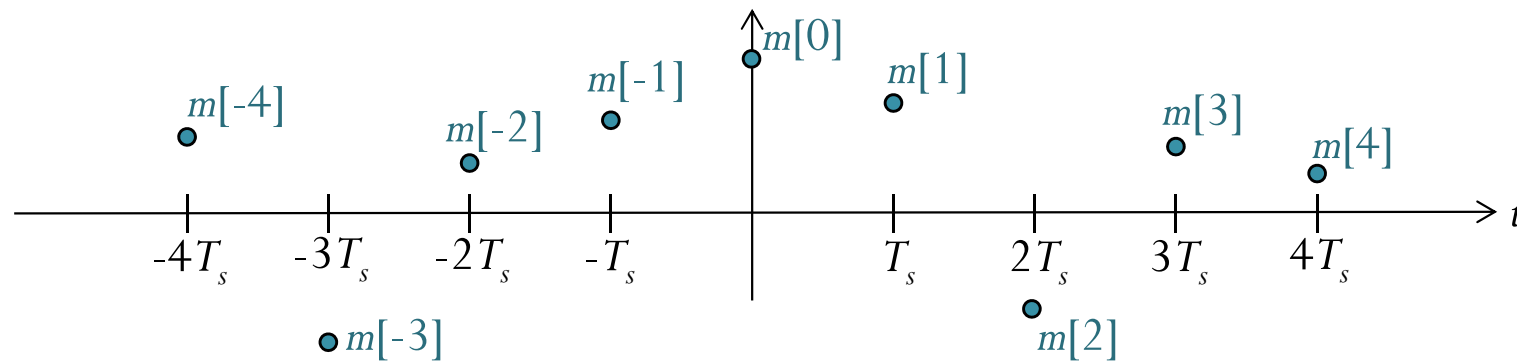
Sampling

- Record the value every T_s seconds.



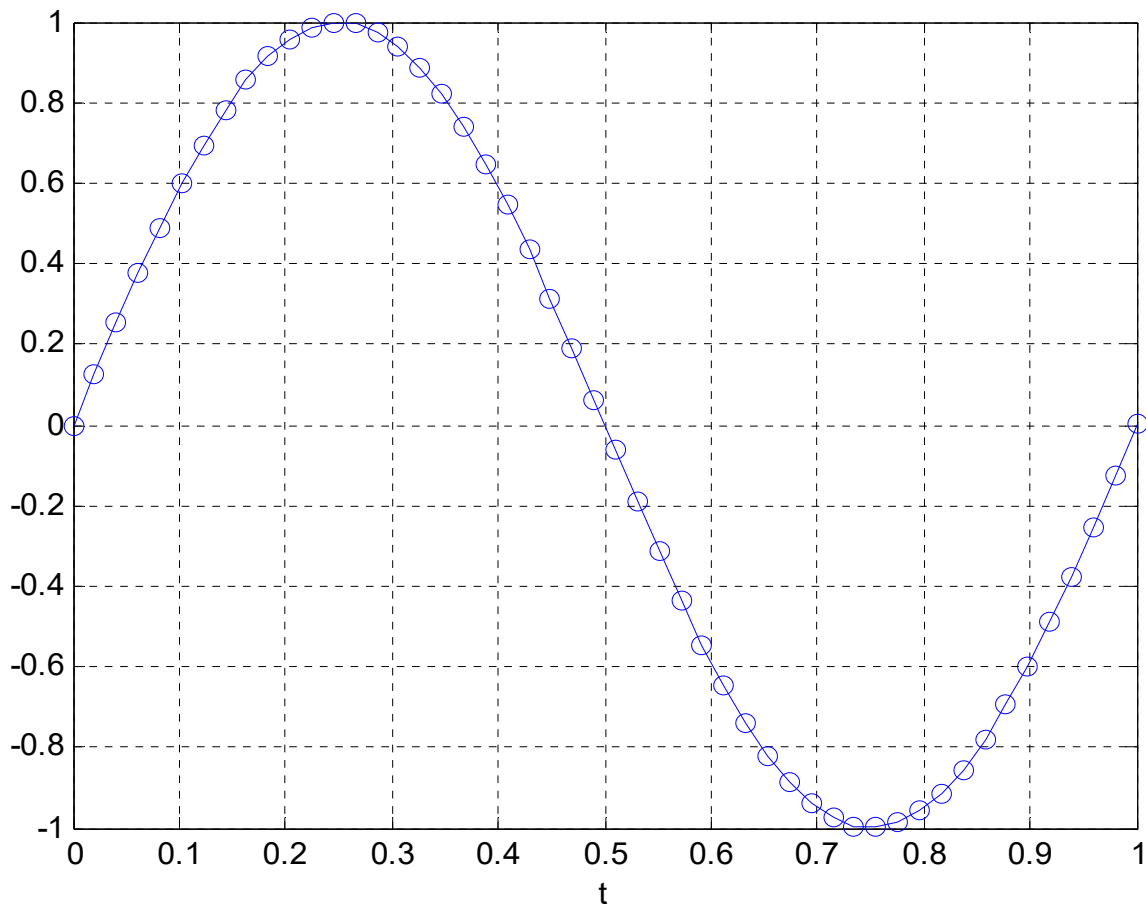
Sampling

- Get a sequence of samples (numbers).



Example: Plotting $\sin(100\pi t)$ (1/6)

This is the plot of $\sin(100\pi t)$. What's wrong with it?



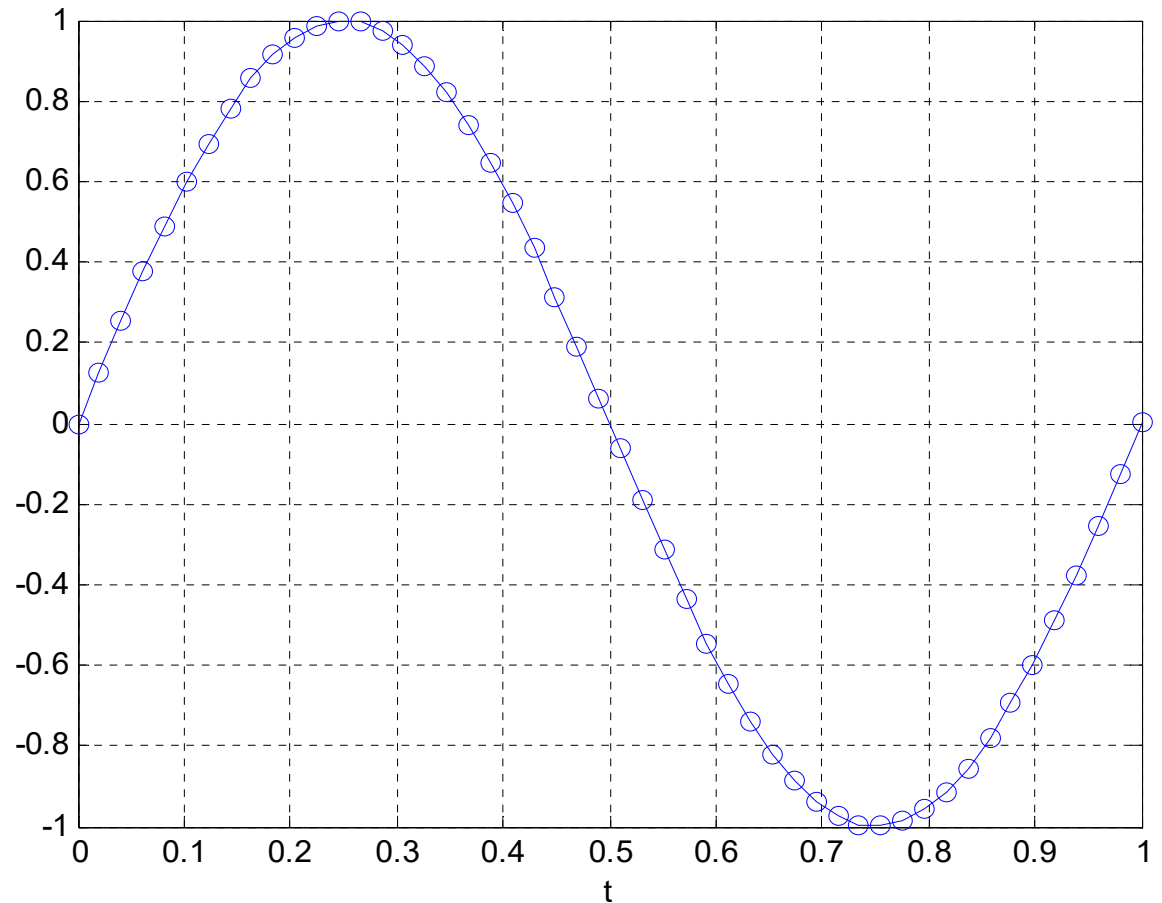
[AliasingSin_FirstEx.m]



Example: Plotting $\sin(100\pi t)$ (2/6)

- Plot 50 points from 0 to 1.

```
close all; clear all;  
fs = 49;  
ET = 1;  
t = 0:1/fs:ET;  
x = sin(100*pi*t);  
plot(t,x,'-o'); grid on  
xlabel('t')
```



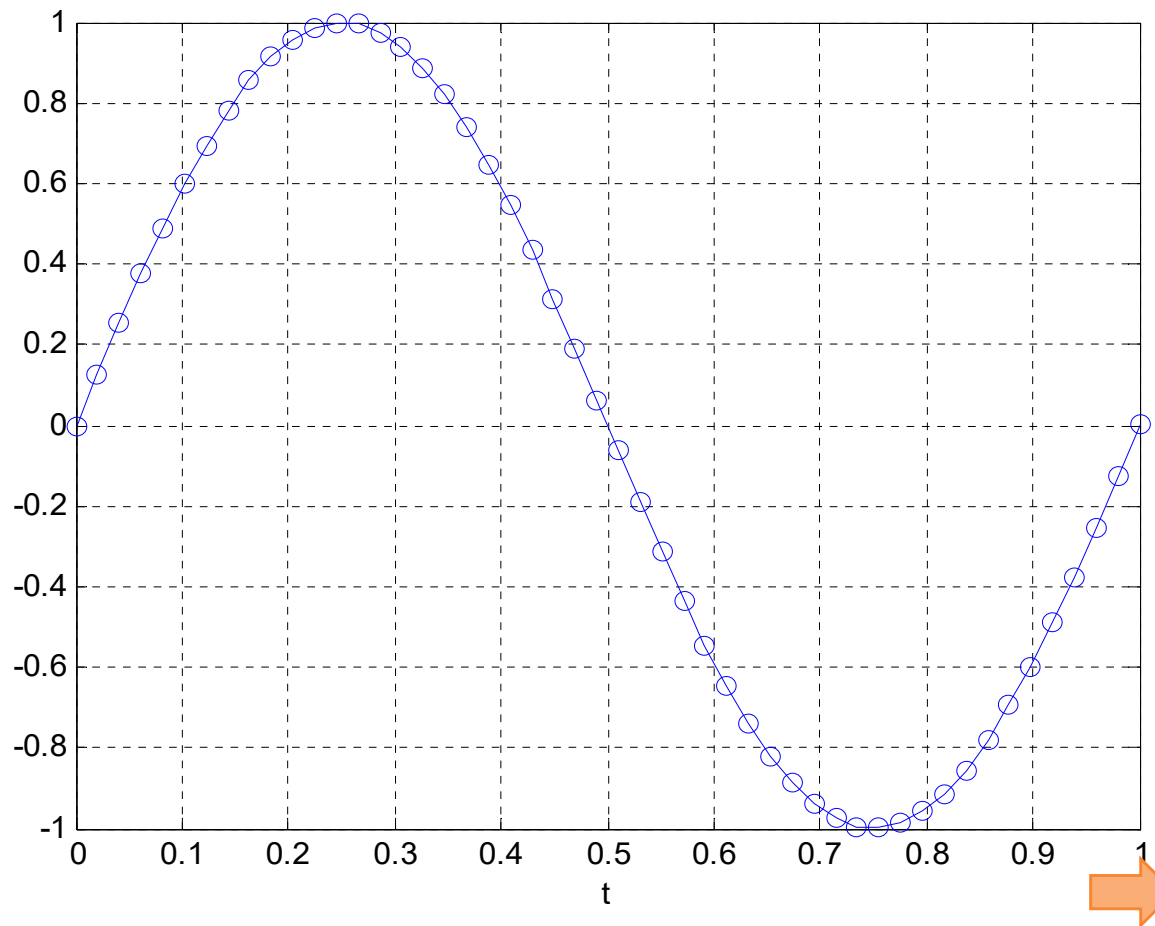
Example: Plotting $\sin(100\pi t)$ (3/6)

Signal of the form $\sin(2\pi f_0 t)$ have frequency $f = f_0$ Hz.

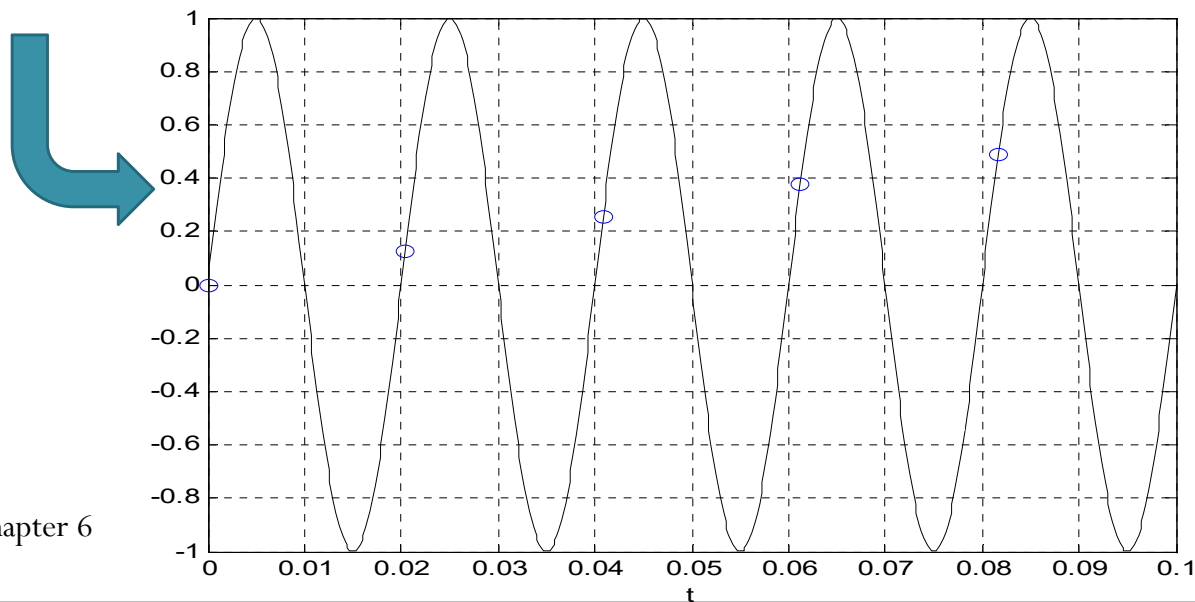
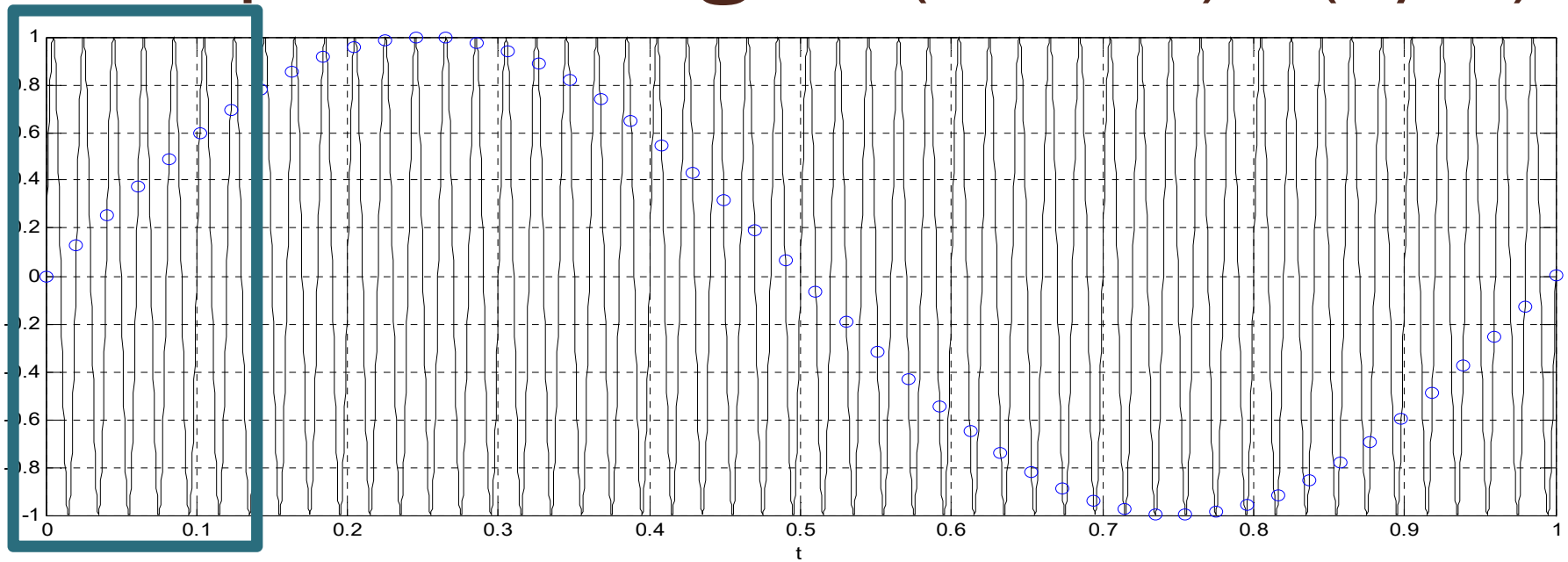
So, the frequency of $\sin(100\pi t)$ is 50 Hz.

From time 0 to 1, it should have completed 50 cycles. However, our plot has only one cycle.

It looks more like the plot of $\sin(2\pi t)$



Example: Plotting $\sin(100\pi t)$ (4/6)



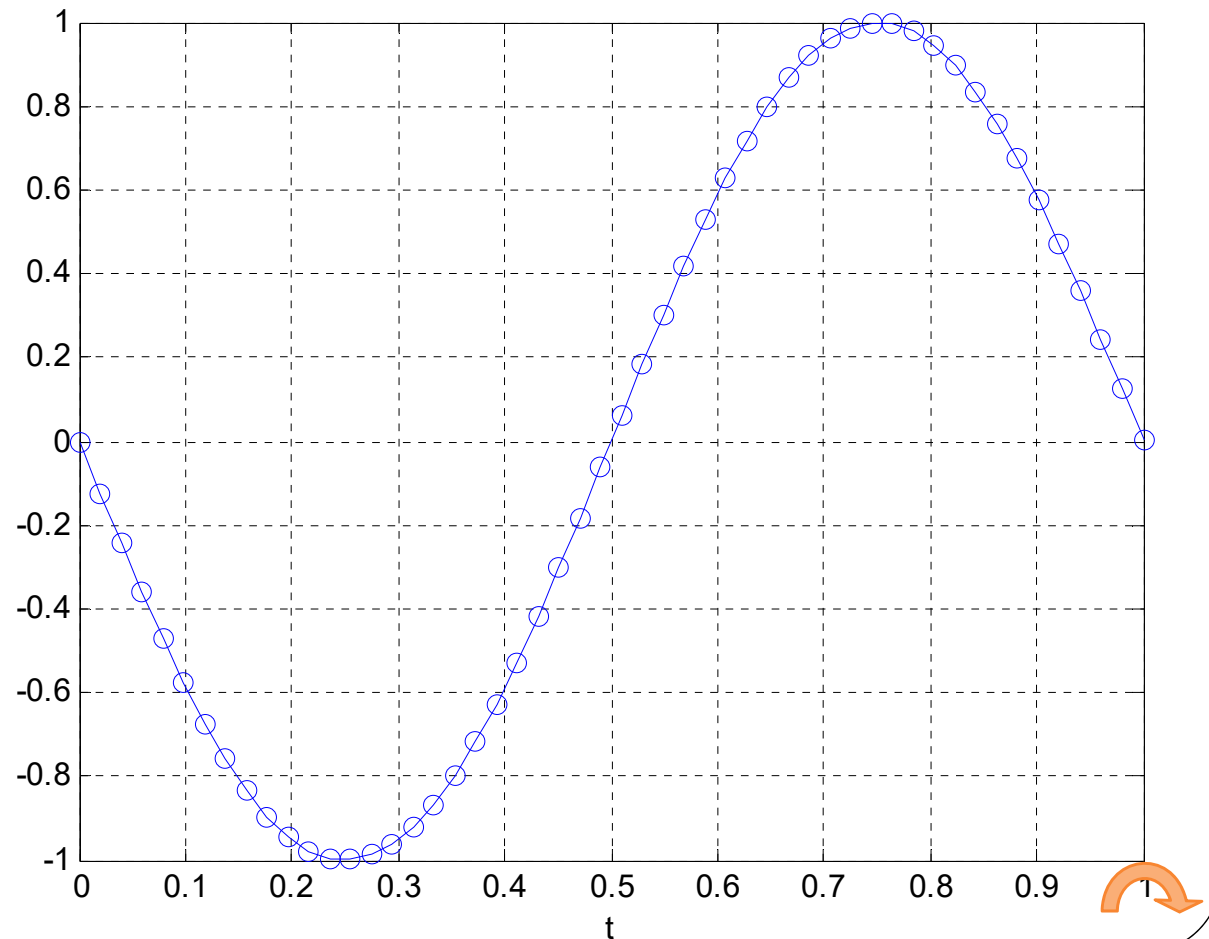
Aliasing causes high-frequency signal to be seen as low frequency.



Example: Plotting $\sin(100\pi t)$ (5/6)

- Plot 52 points from 0 to 1.

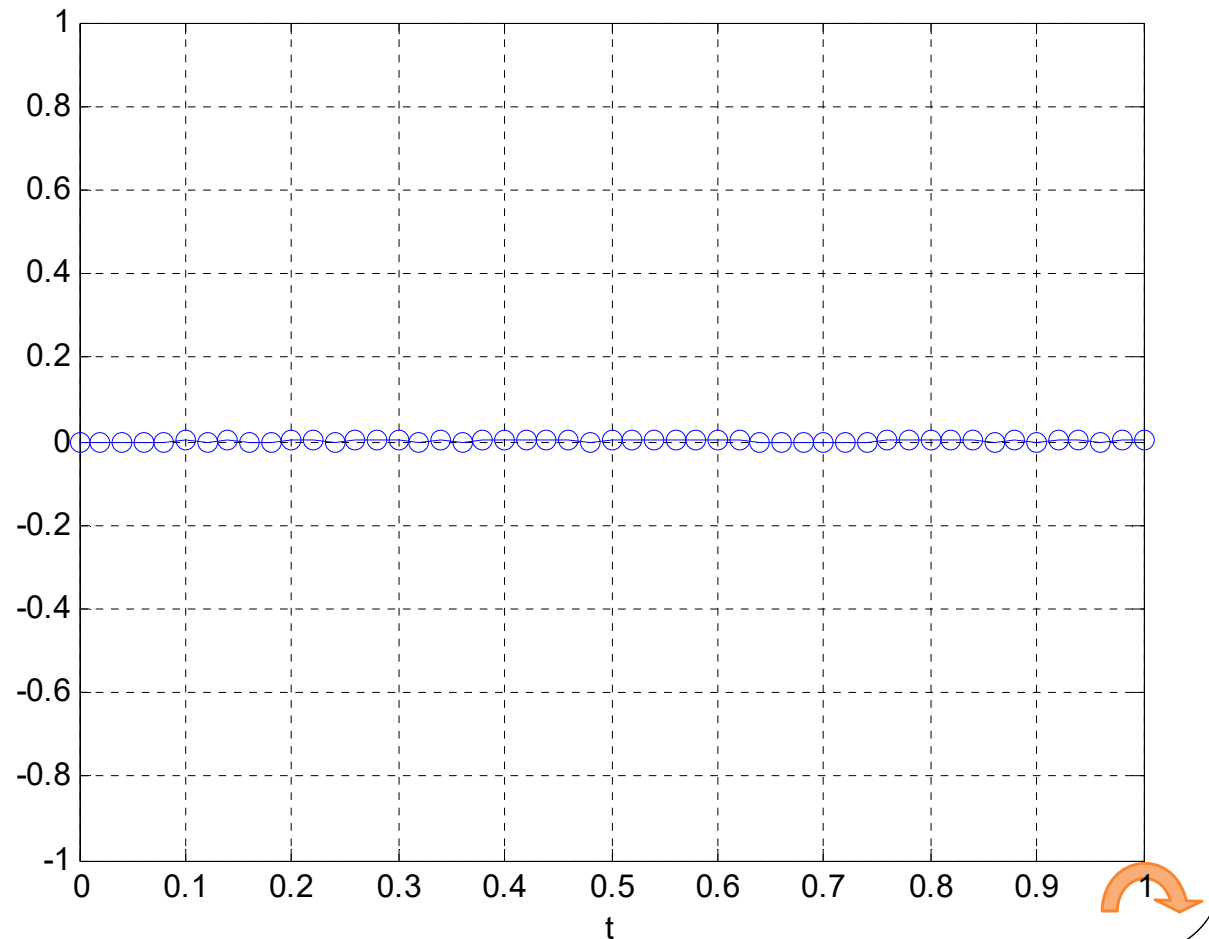
```
close all; clear all;  
fs = 51;  
ET = 1;  
t = 0:1/fs:ET;  
x = sin(100*pi*t);  
plot(t,x,'-o'); grid on  
xlabel('t')
```



Example: Plotting $\sin(100\pi t)$ (6/6)

- Plot 51 points from 0 to 1.

```
close all; clear all;  
fs = 50;  
ET = 1;  
t = 0:1/fs:ET;  
x = sin(100*pi*t);  
plot(t,x,'-o'); grid on  
xlabel('t')  
ylim([-1 1])
```



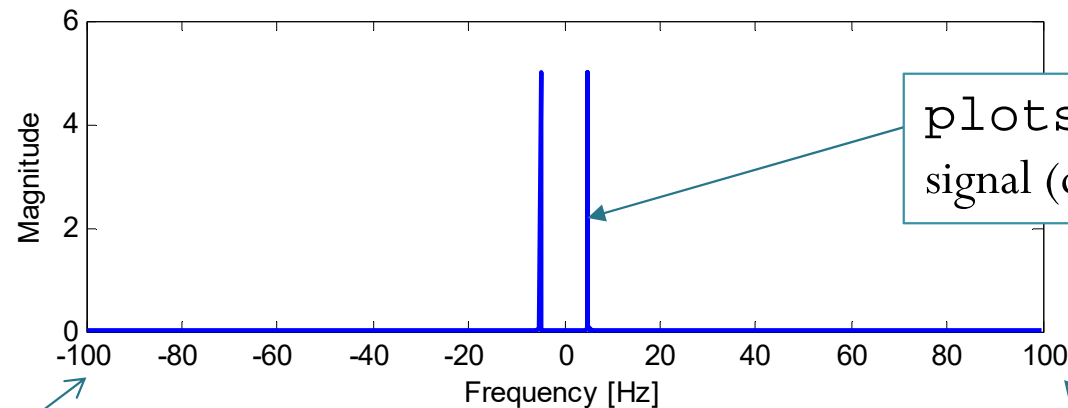
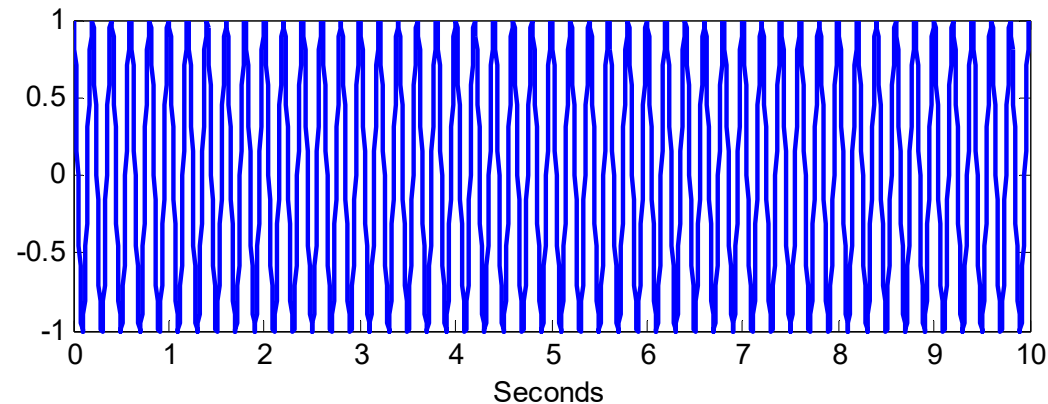
Example 6.10



Using `plotspect.m` to study aliasing

- f_s : Sampling frequency = 200 samples/sec

$$\cos(2\pi(5)t)$$



$$-\frac{f_s}{2}$$

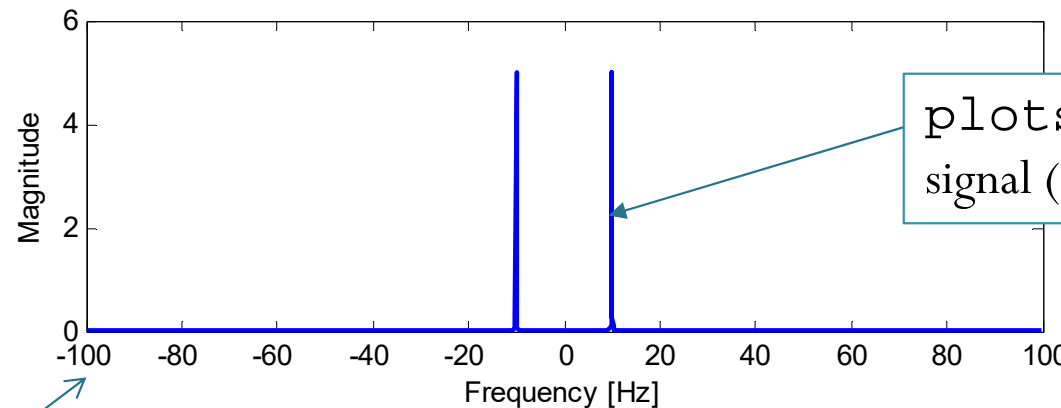
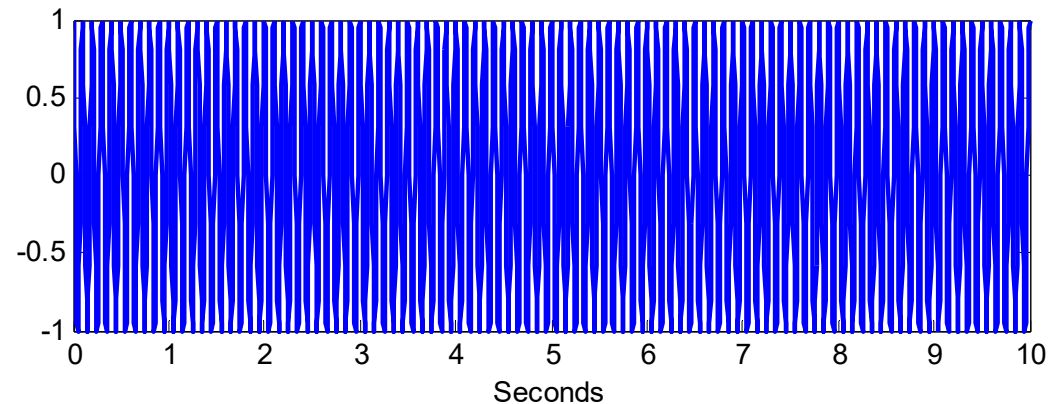
$$\frac{f_s}{2}$$



Using plotspect.m to study aliasing

- f_s : Sampling frequency = 200 samples/sec

$$\cos(2\pi(10)t)$$



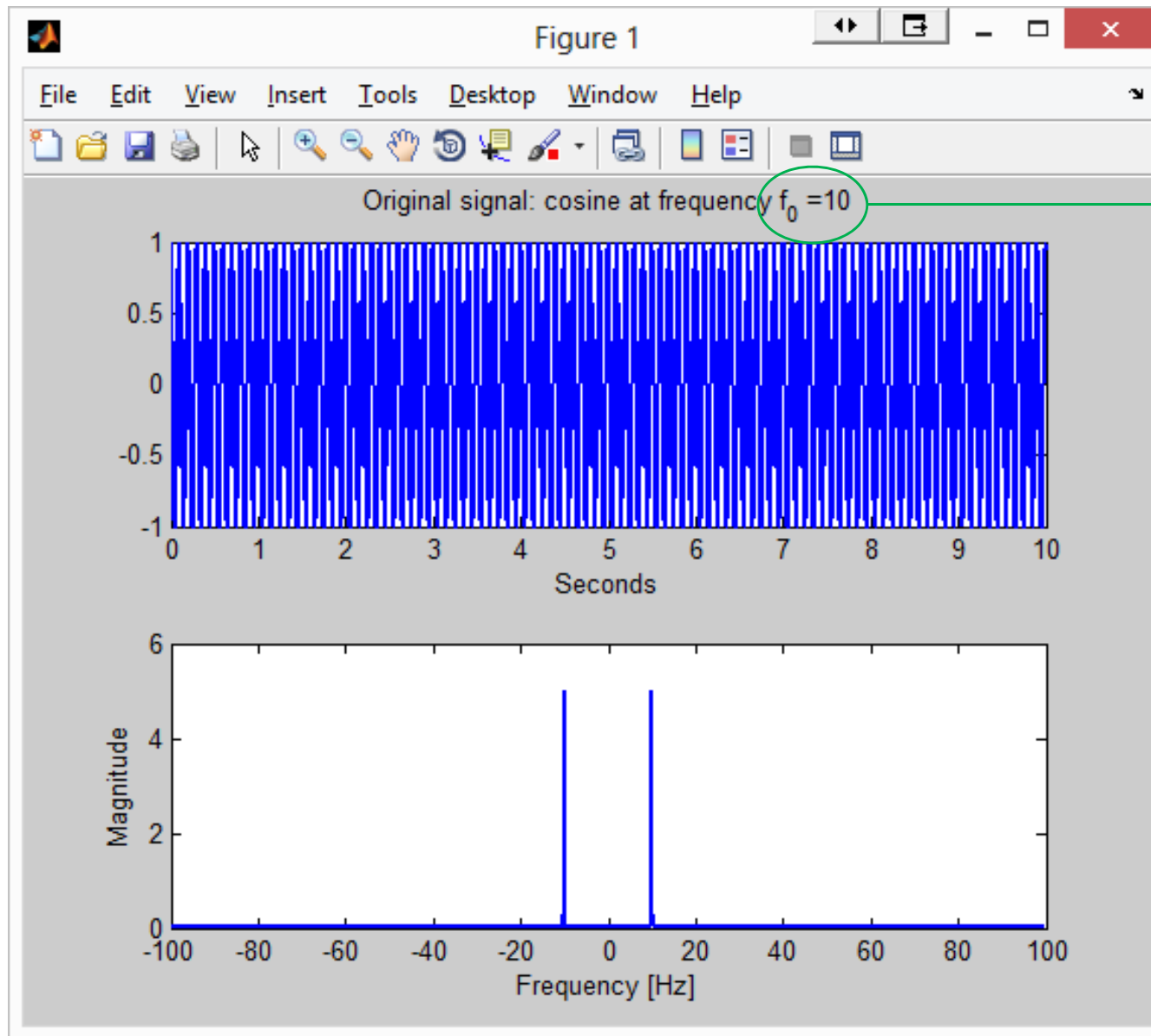
$$-\frac{f_s}{2}$$

$$\frac{f_s}{2}$$



MATLAB Demo

f_s : Sampling frequency = 200 samples/sec

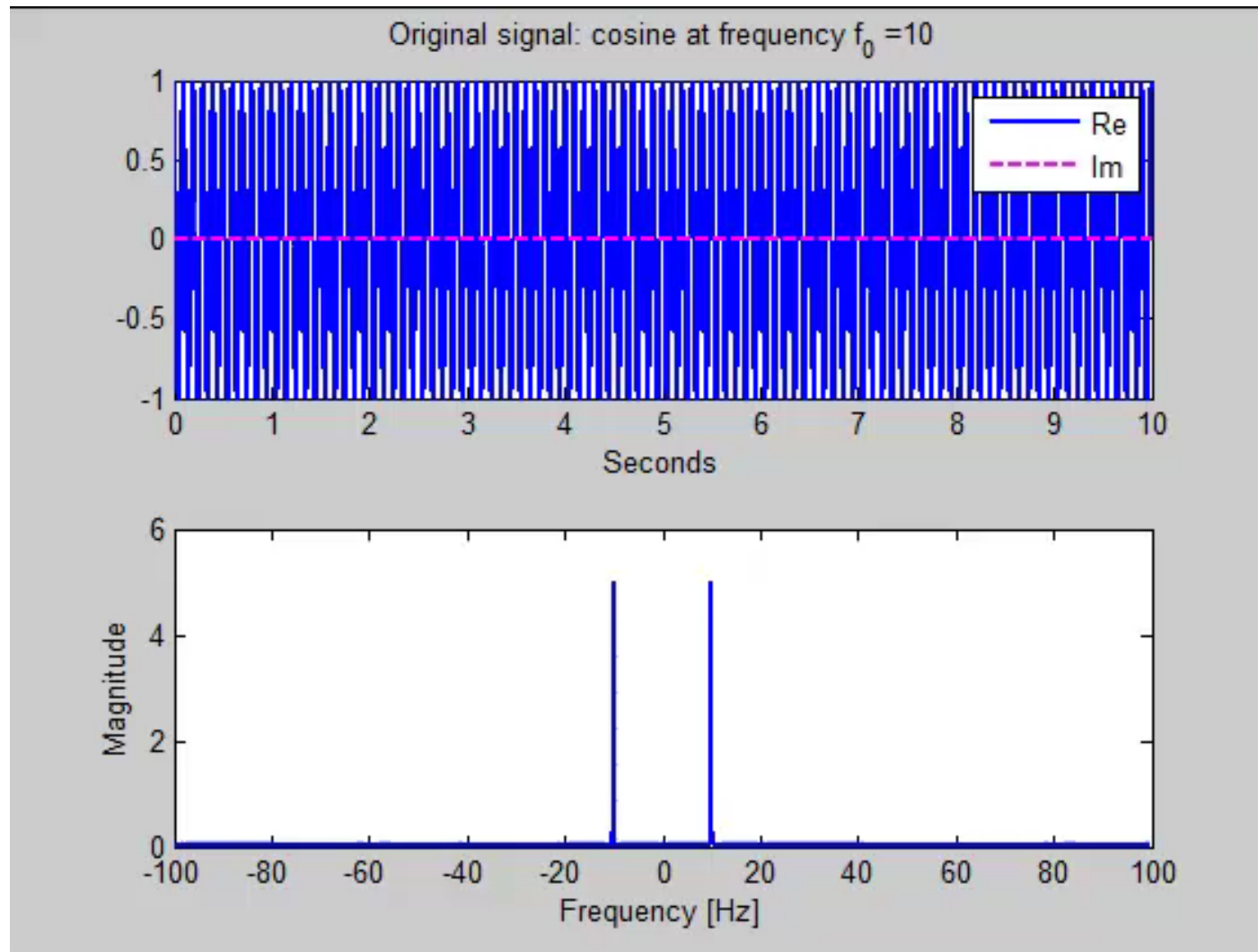


$$\cos(2\pi(f_0)t)$$

The frequency f_0 of the cosine will be increased (in steps of 10) from 10 Hz to 300 Hz.

[aliasingCos.m] 

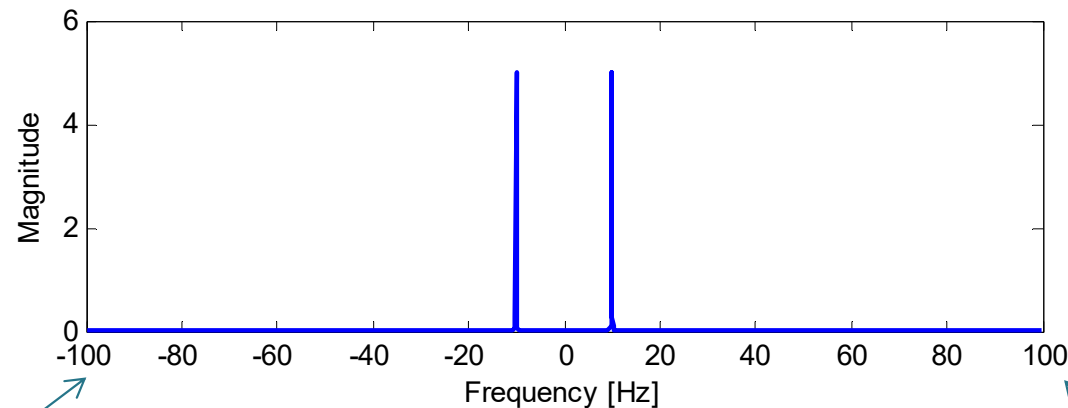
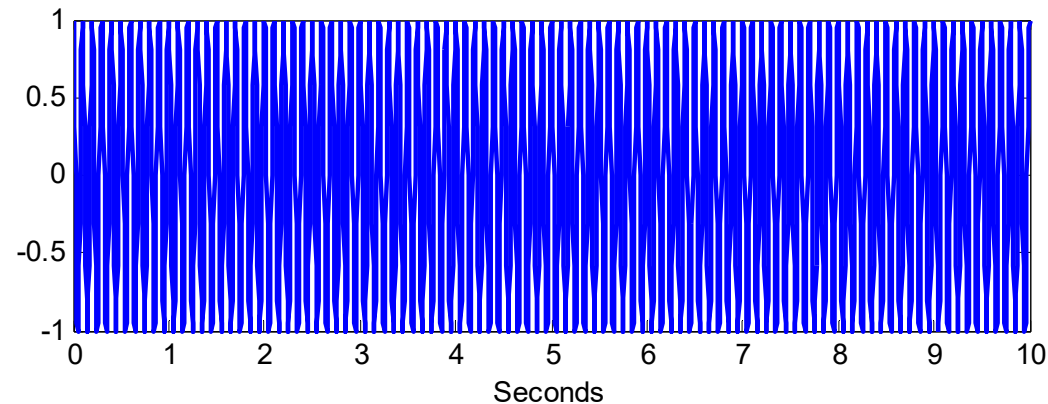
MATLAB Demo



Using plotspect.m to study aliasing

- f_s : Sampling frequency = 200 samples/sec

$$\cos(2\pi(10)t)$$



$$-\frac{f_s}{2}$$

$$\frac{f_s}{2}$$

In the subsequent plots, we will show only the frequency-domain part.

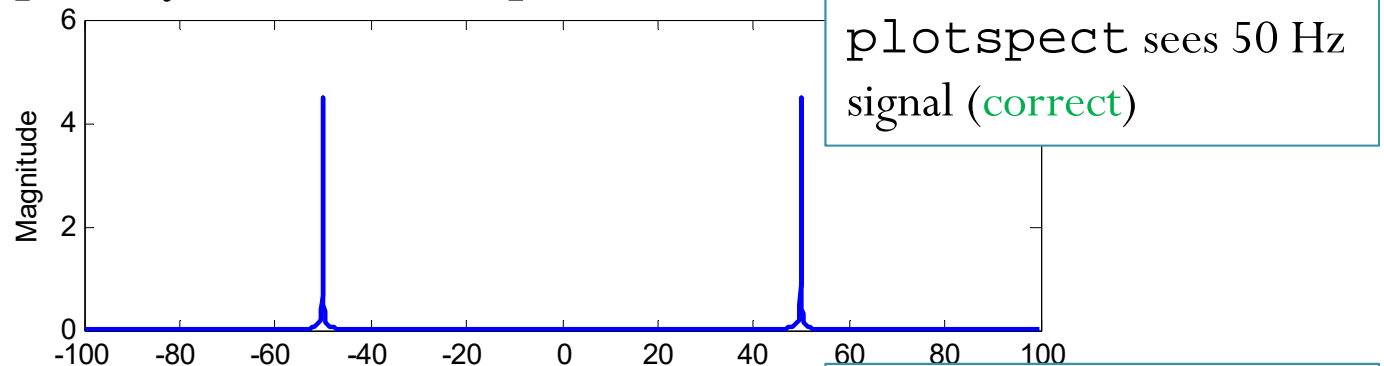


Figure 46

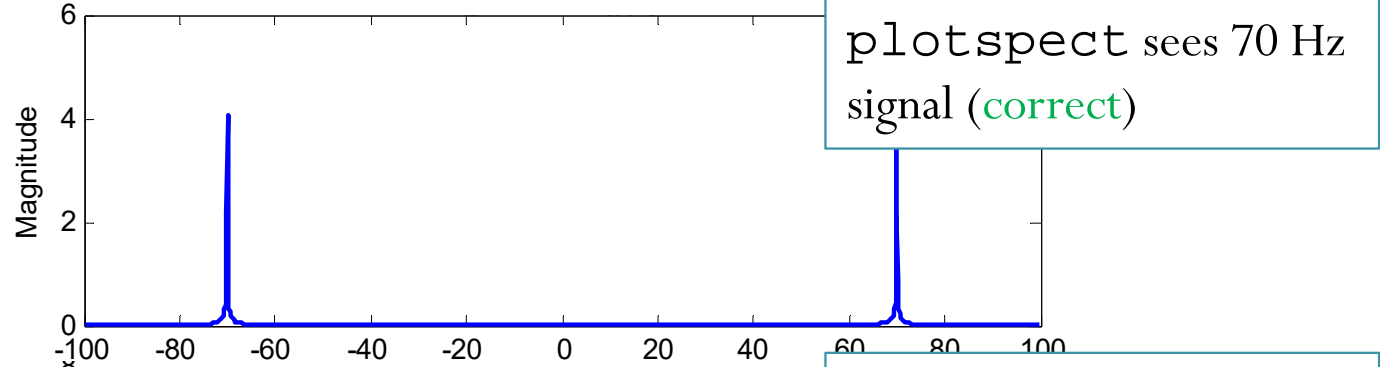
Using plotspect.m to study aliasing

- f_s : Sampling frequency = 200 samples/sec

$$\cos(2\pi(50)t)$$



$$\cos(2\pi(70)t)$$



$$\cos(2\pi(100)t)$$

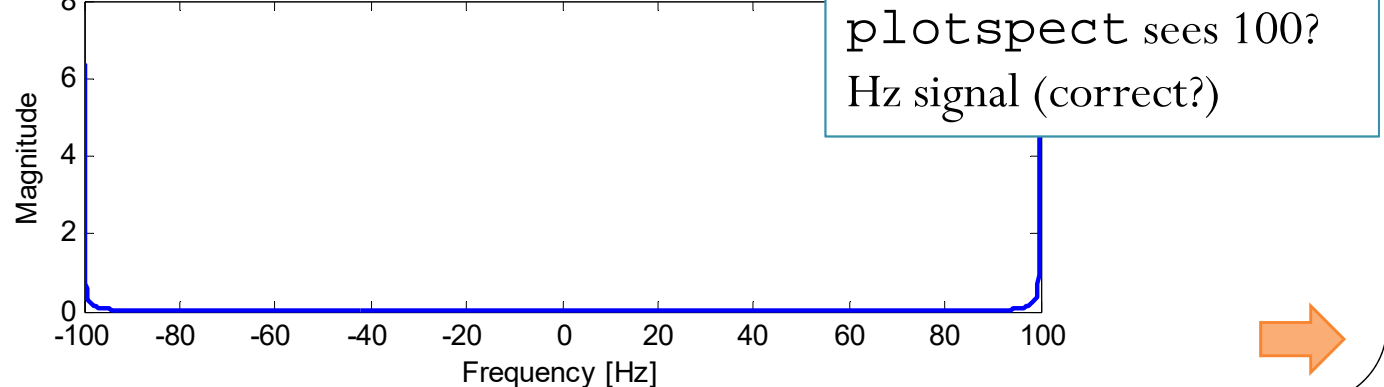
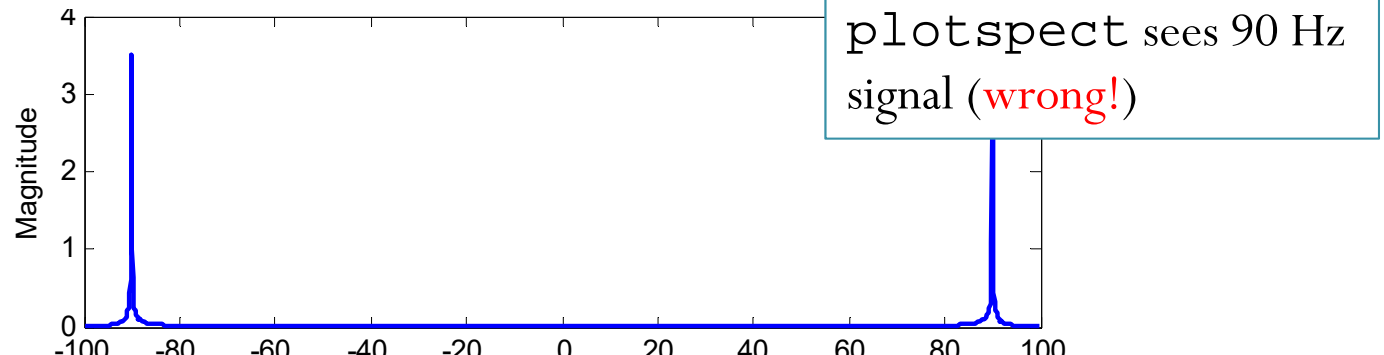


Figure 46

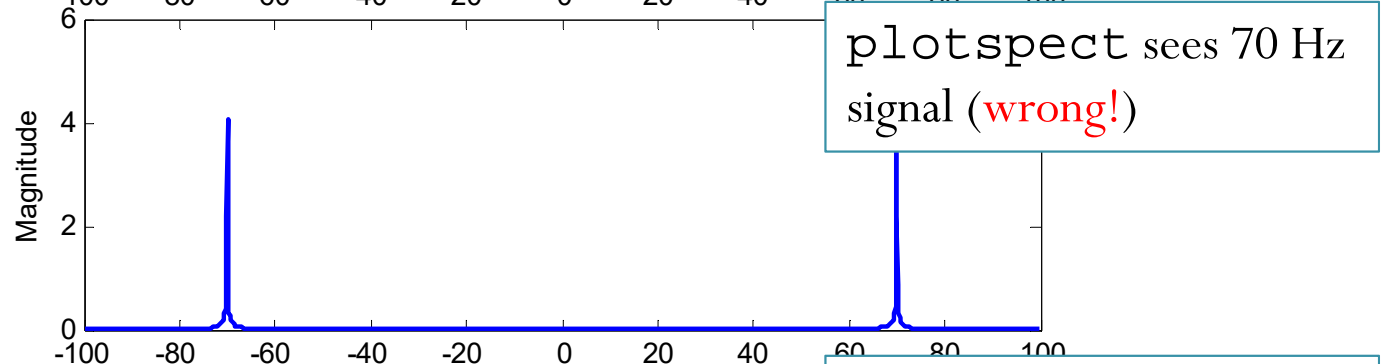
Using plotspect.m to study aliasing

- f_s : Sampling frequency = 200 samples/sec

$$\cos(2\pi(110)t)$$



$$\cos(2\pi(130)t)$$



$$\cos(2\pi(190)t)$$

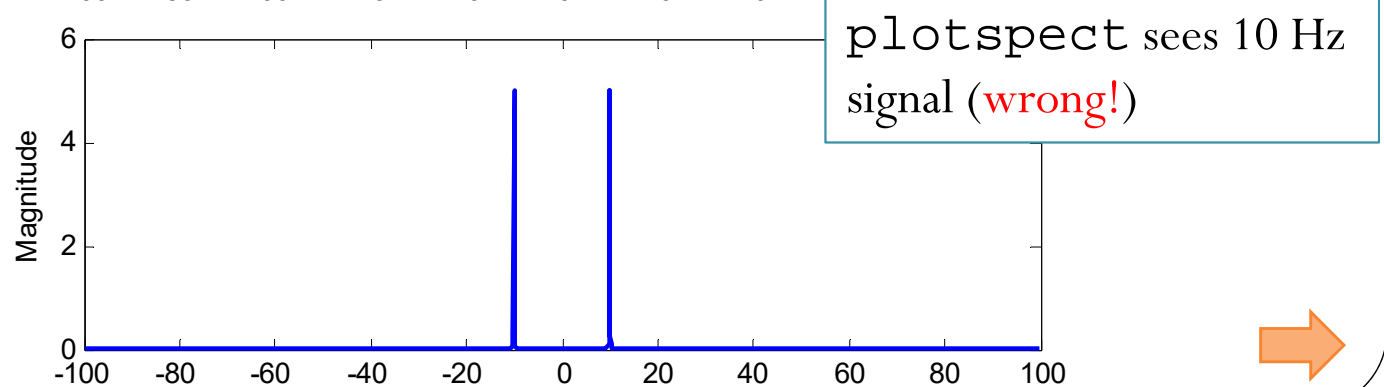


Figure 46

Using plotspect.m to study aliasing

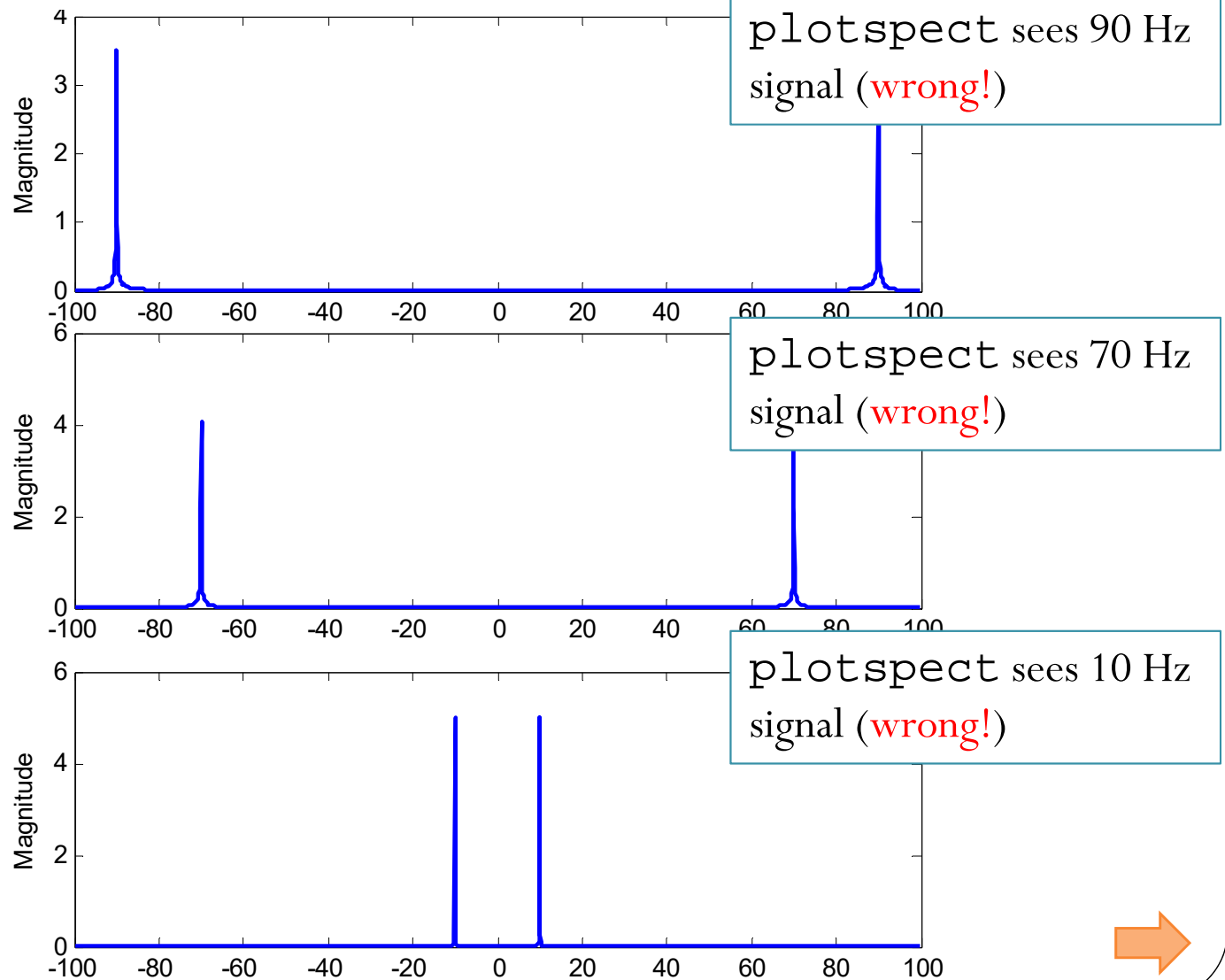
- f_s : Sampling frequency = 200 samples/sec

$$\cos(2\pi(110)t)$$

This behavior is commonly referred to as **folding**.

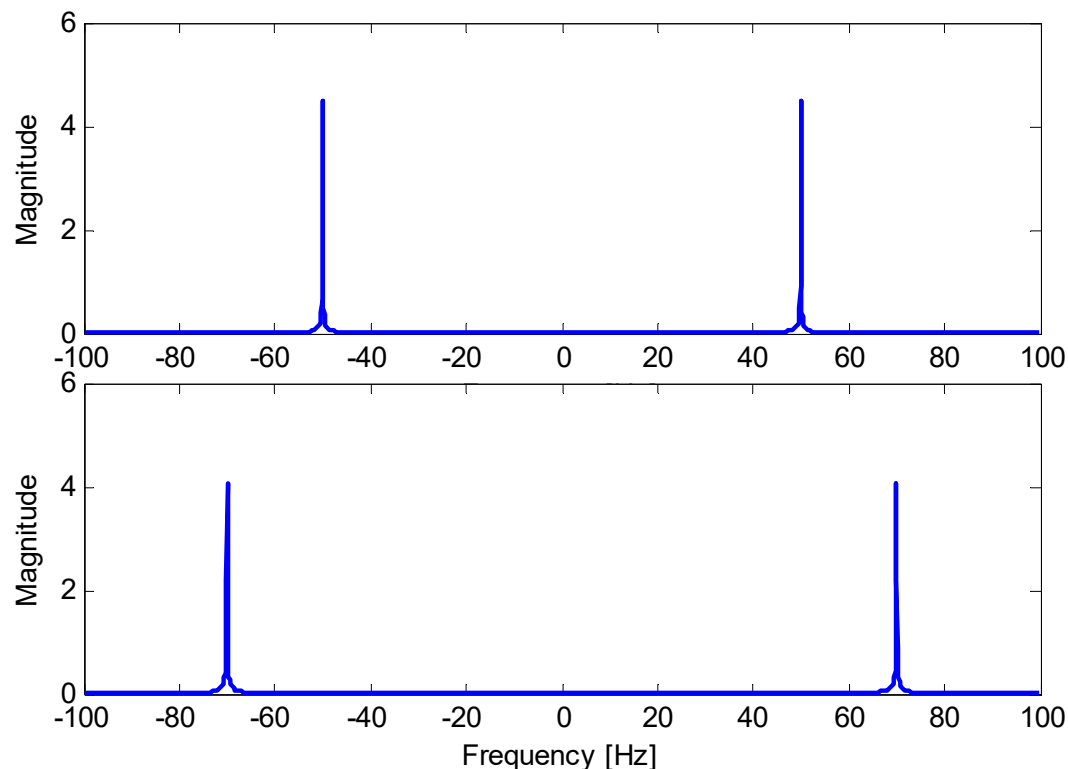
$$\cos(2\pi(130)t)$$

$$\cos(2\pi(190)t)$$

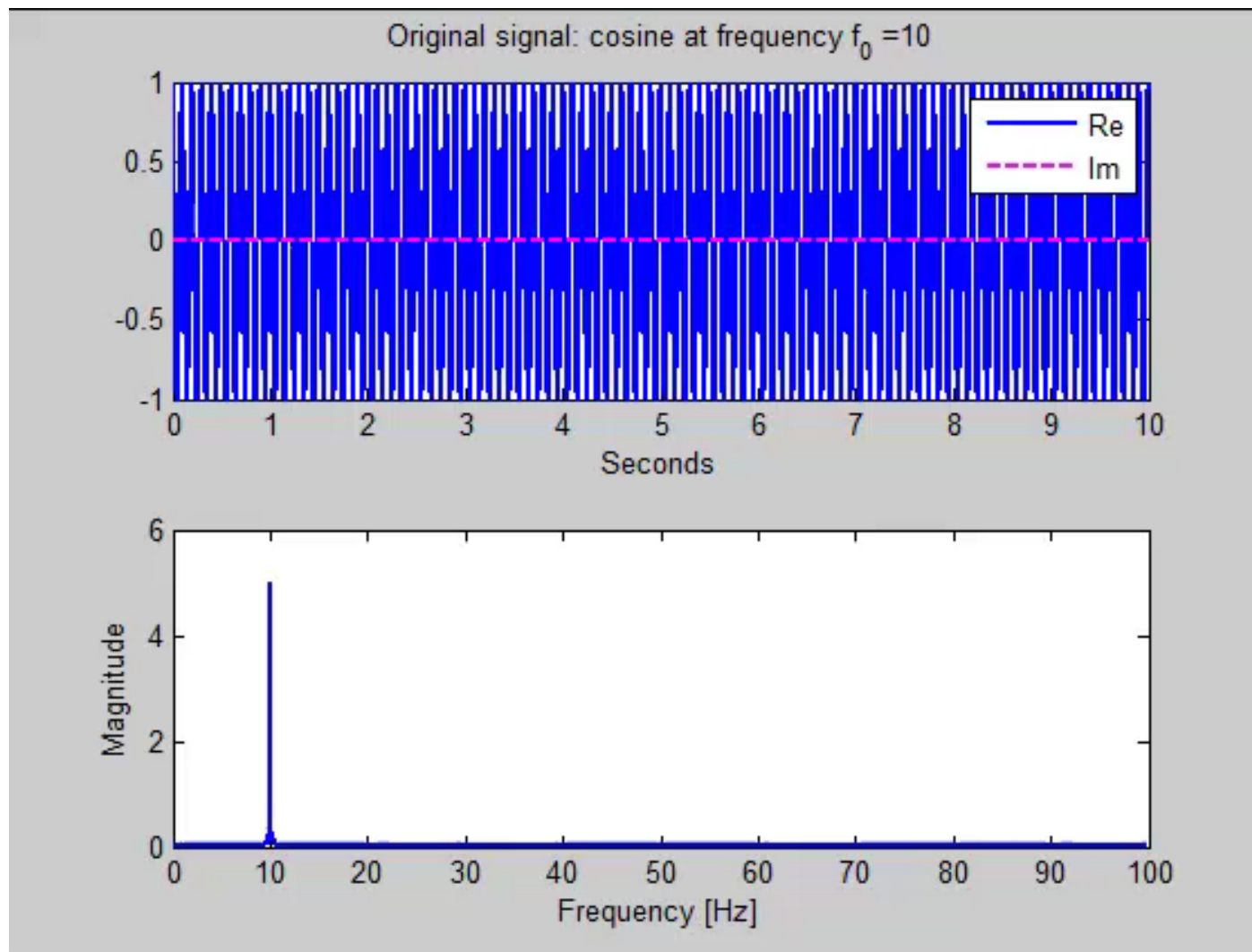


The folding technique

- The even symmetry of the $\cos(2\pi(f_0)t)$ spectrum means that we only have to look at positive frequency to find its perceived frequency



The folding technique

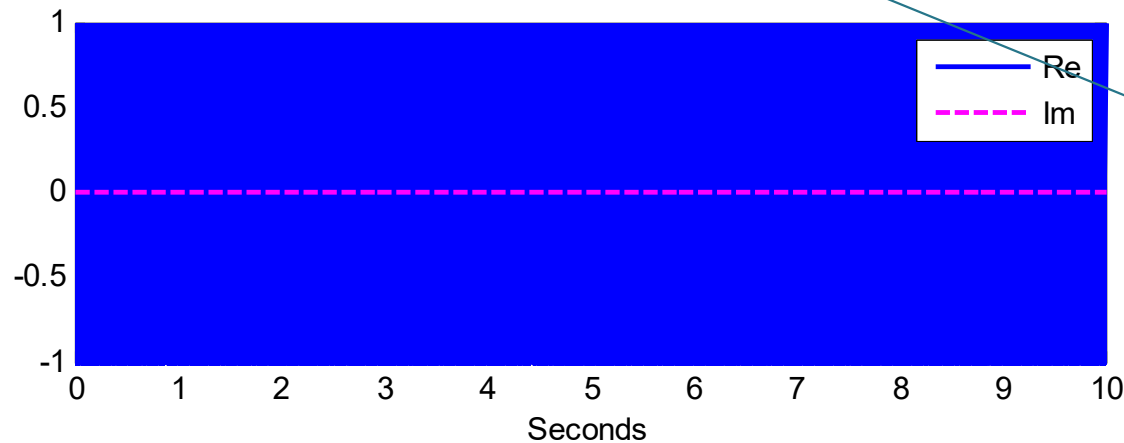


The folding technique

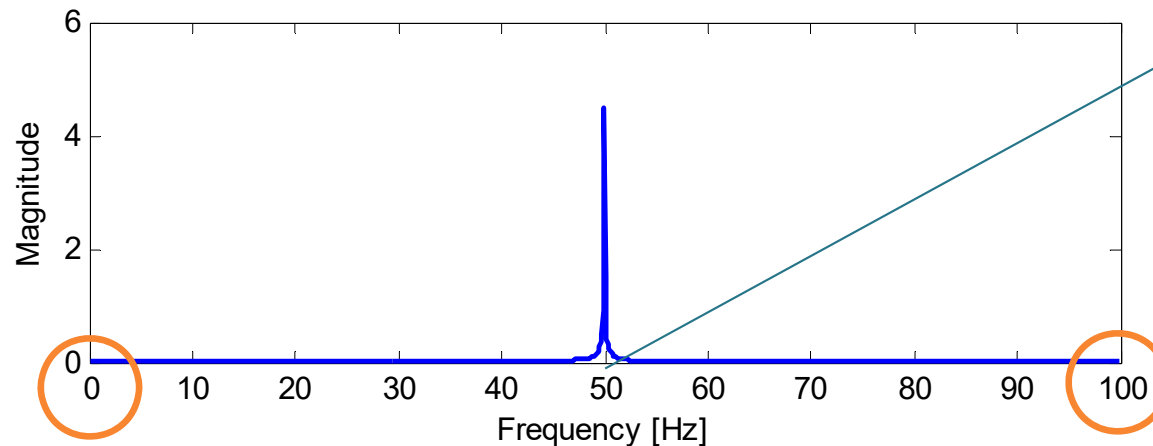
- The folding technique is useful for finding the perceived frequency of $\cos(2\pi(f_0)t)$.

Demo: [aliasingCos_folding]

Original signal: cosine at frequency $f_0 = 150$



When $f_s = 200$ [Sa/s], the cosine @ freq. 150 Hz will be perceived as a cosine @ freq. 50 Hz.



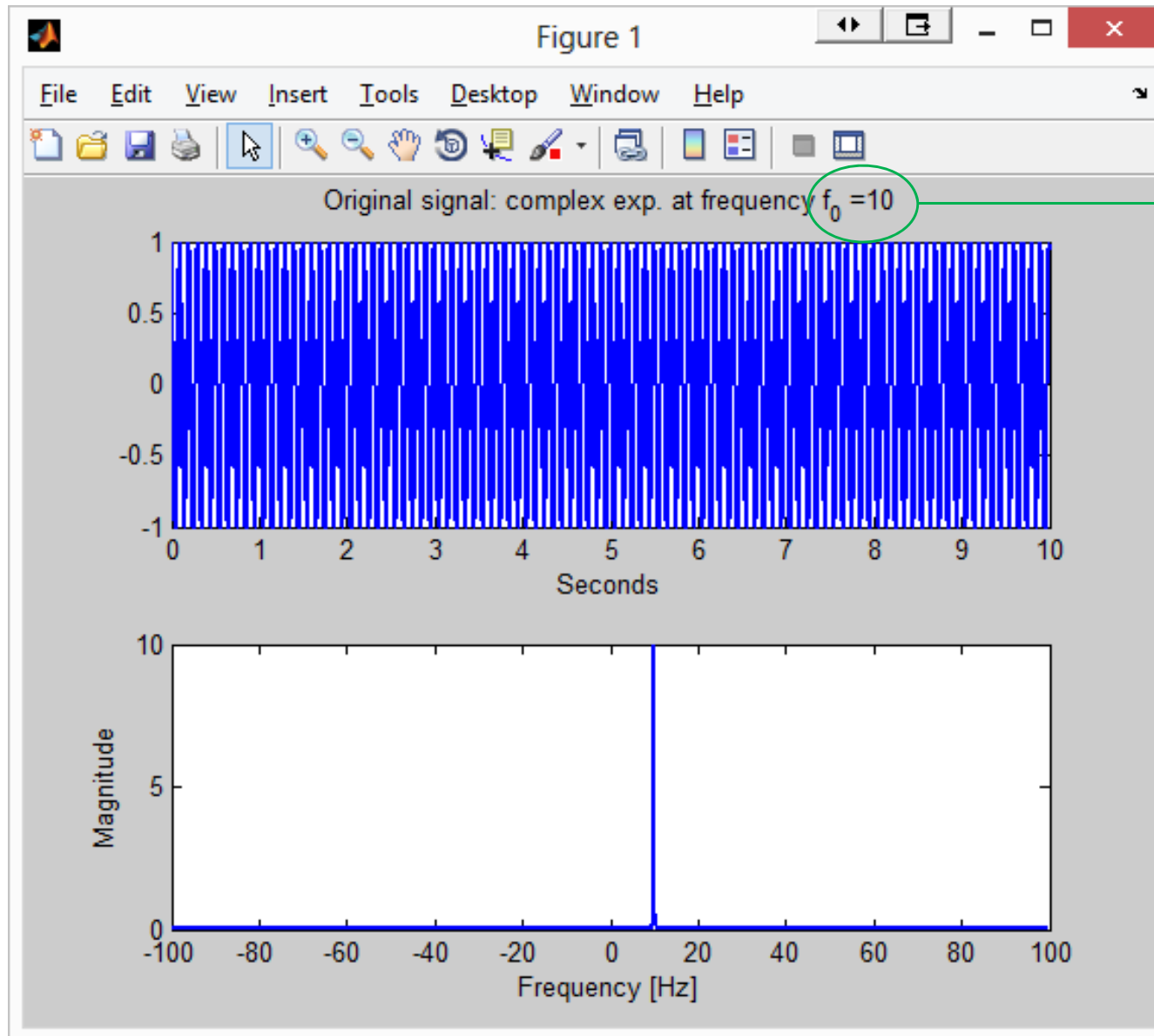
Pac Man's Tunneling

Actually, the delta functions are doing **tunneling** (like in Pac Man).



MATLAB Demo

f_s : Sampling frequency = 200 samples/sec

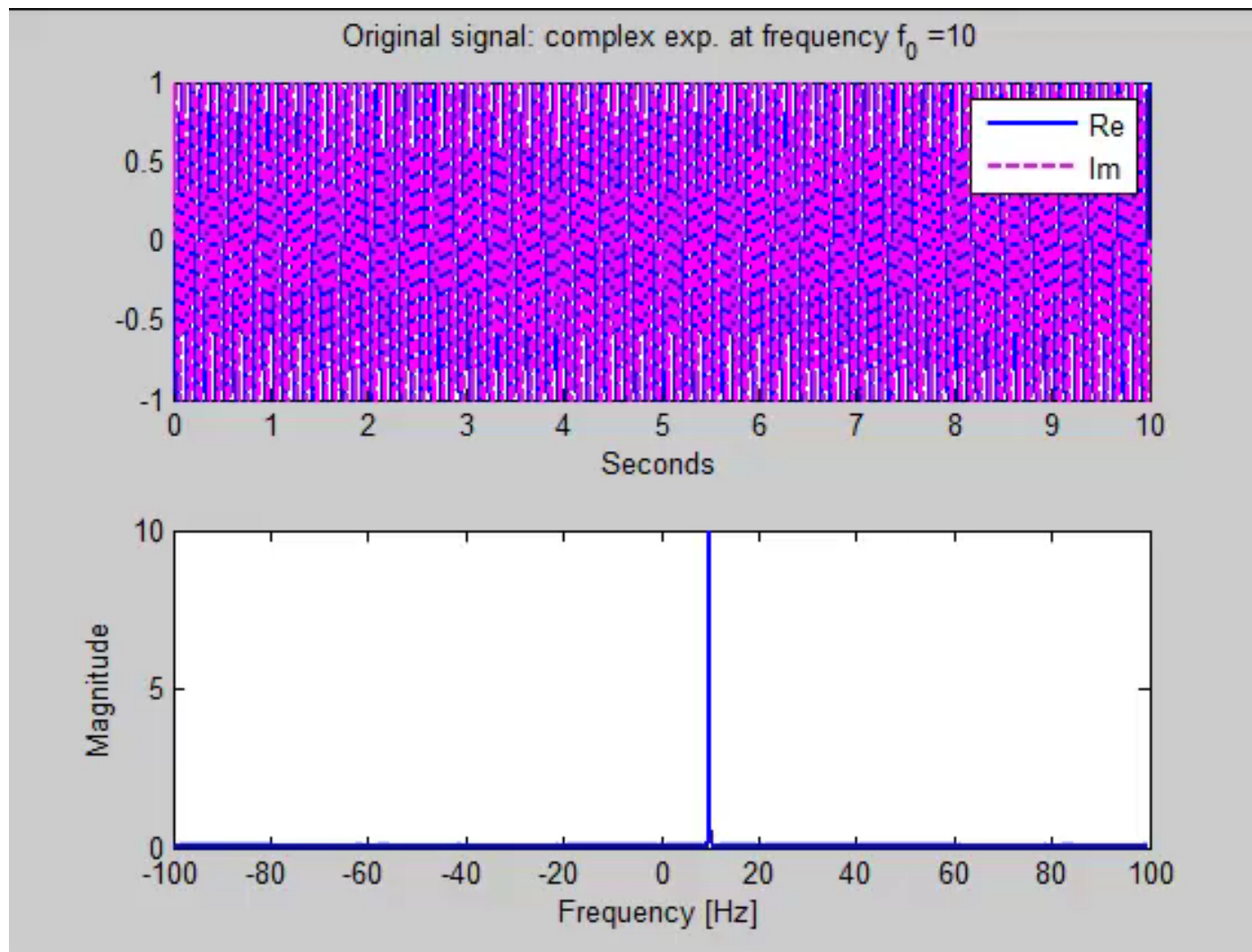


$$e^{j2\pi(f_0)t}$$

The frequency f_0 of the complex expo. signal is increased (in steps of 10) from 10 Hz to 300 Hz.

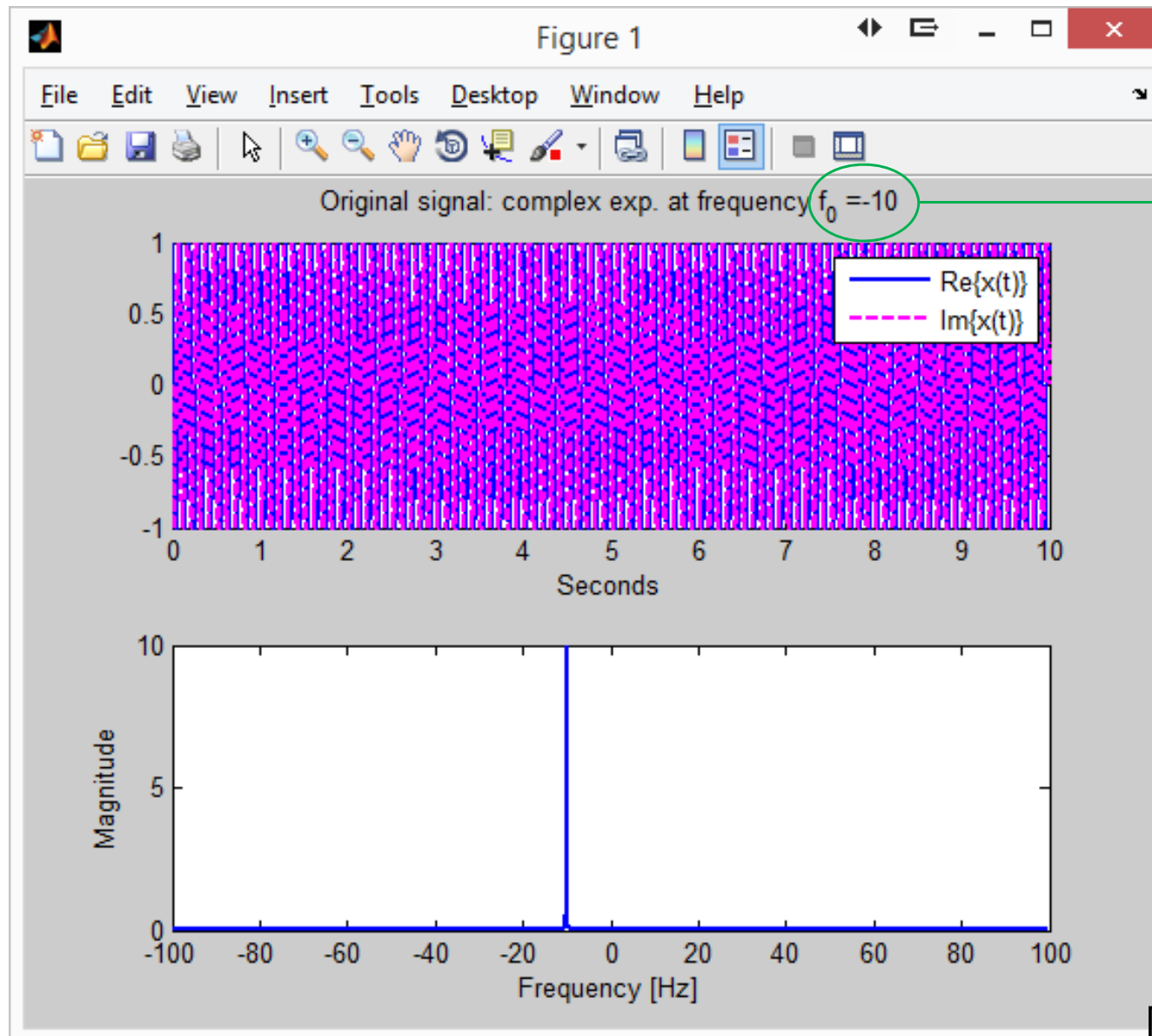
[aliasingExp.m] 

MATLAB Demo



MATLAB Demo

f_s : Sampling frequency = 200 samples/sec

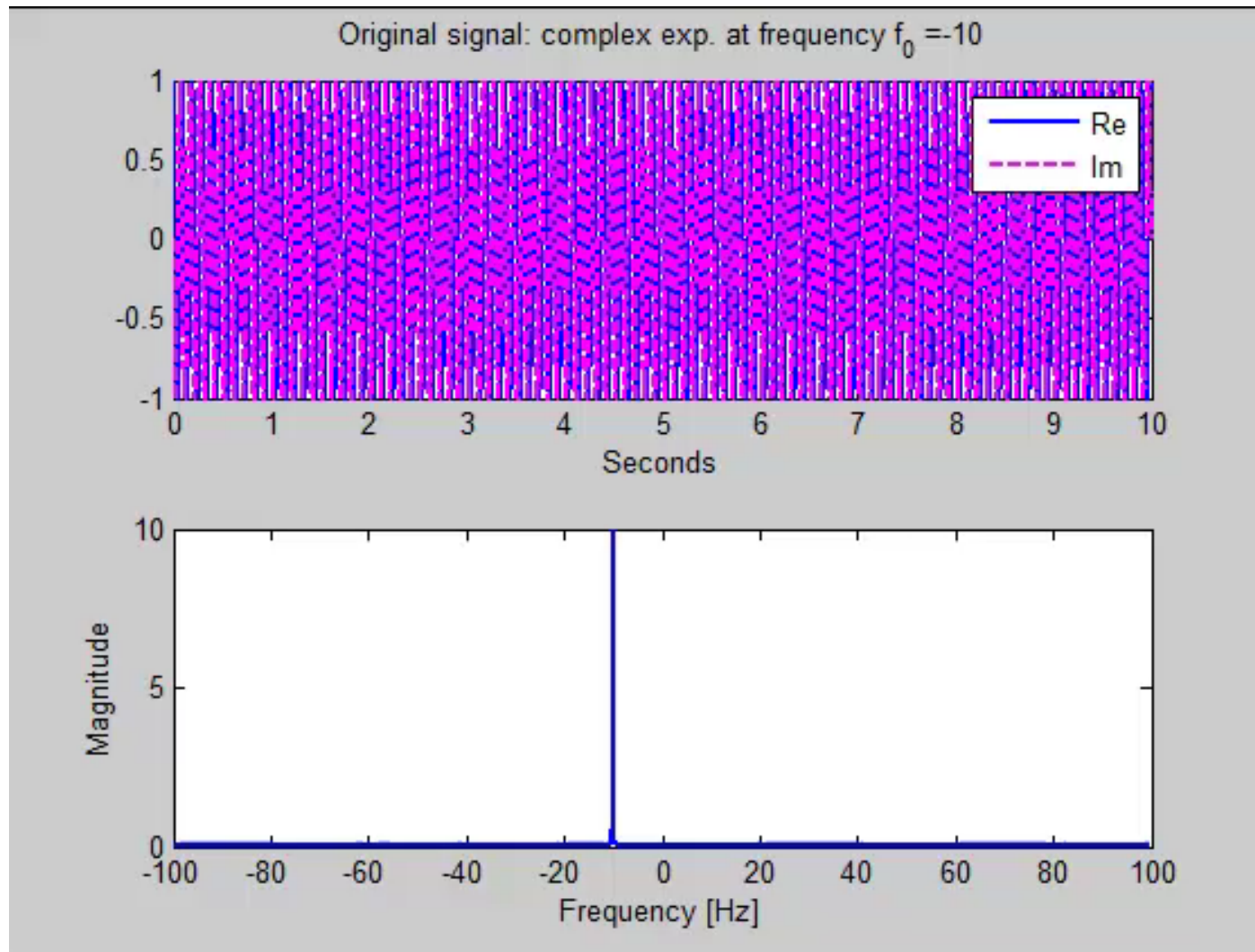


$$e^{j2\pi(f_0)t}$$

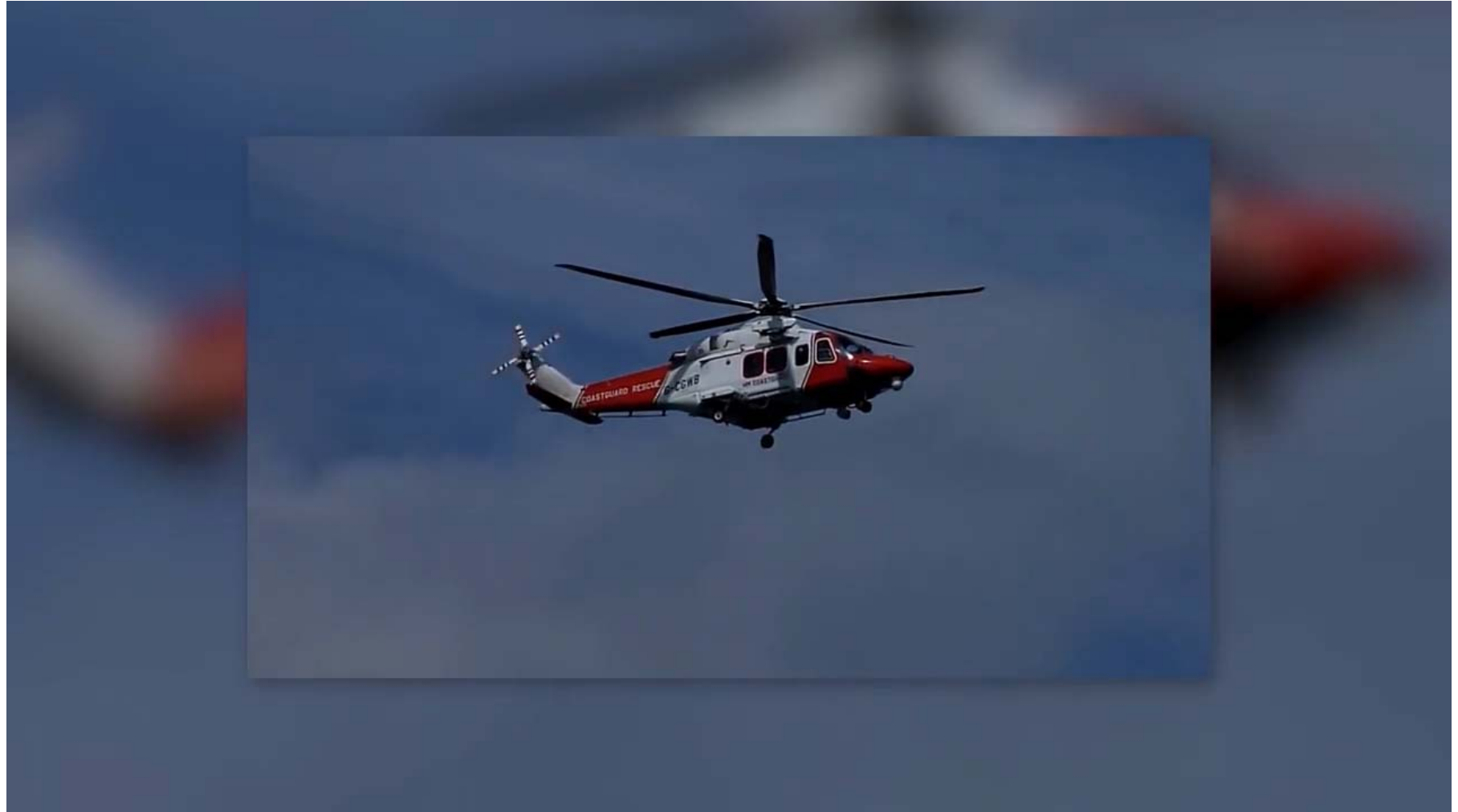
The frequency f_0 of the **complex expo. signal** will be decreased (in steps of 10) from **-10 Hz to -300 Hz**.

[aliasingExpNegative.m] 

MATLAB Demo



Helicopter Blades Can Look Strange On Video



Video as Succession of Still Images



Frame Rate



Why car wheels rotate backwards in movies?



Now You See Me 2 Rain Scene



Sampling via the Camera



Sampling via the Camera



Sampling via the Camera



Sampling via the Camera



Sampling via Strobe Light



Sampling via Strobe Light



Sampling via Strobe Light

